

Marks
5

- Nickel metal can be extracted and recycled from mobile phone batteries. This process leads to solutions containing both $\text{Cu}^{2+}(\text{aq})$ and $\text{Ni}^{2+}(\text{aq})$ ions. Separation of these ions is achieved by adding tiny amounts of sulfide ions as the metal sulfides have low and very different solubilities: $K_{\text{sp}}(\text{CuS}) = 8 \times 10^{-34}$ and $K_{\text{sp}}(\text{NiS}) = 3 \times 10^{-19}$.

An aqueous solution has $[\text{Ni}^{2+}(\text{aq})] = 0.0100 \text{ M}$ and an unknown concentration of $\text{Cu}^{2+}(\text{aq})$ ions. $\text{S}^{2-}(\text{aq})$ ions are added in small increments. CuS begins to precipitate when $[\text{S}^{2-}(\text{aq})] = 8 \times 10^{-32} \text{ M}$. What was the original value of $[\text{Cu}^{2+}(\text{aq})]$?

The solubility of CuS is *much* lower than NiS as its K_{sp} value is *much* smaller. When CuS begins to precipitate, virtually none will be left in solution.

$\text{CuS}(\text{s})$ dissolves to give $\text{Cu}^{2+}(\text{aq})$ and $\text{S}^{2-}(\text{aq})$, so $K_{\text{sp}}(\text{CuS}) = [\text{Cu}^{2+}(\text{aq})][\text{S}^{2-}(\text{aq})]$.

As $K_{\text{sp}} = 8 \times 10^{-34}$ and precipitation occurs when $[\text{S}^{2-}(\text{aq})] = 8 \times 10^{-32} \text{ M}$,

$$[\text{Cu}^{2+}(\text{aq})] = K_{\text{sp}}(\text{CuS}) / [\text{S}^{2-}(\text{aq})] = (8 \times 10^{-34}) / (8 \times 10^{-32}) = 0.01 \text{ M}$$

Answer: **0.01 M**

At what $[\text{S}^{2-}(\text{aq})]$ will NiS precipitate?

$\text{NiS}(\text{s})$ dissolves to give $\text{Ni}^{2+}(\text{aq})$ and $\text{S}^{2-}(\text{aq})$, so $K_{\text{sp}}(\text{NiS}) = [\text{Ni}^{2+}(\text{aq})][\text{S}^{2-}(\text{aq})]$.

As $K_{\text{sp}} = 3 \times 10^{-19}$ and $[\text{Ni}^{2+}(\text{aq})] = 0.0100 \text{ M}$,

$$[\text{S}^{2-}(\text{aq})] = K_{\text{sp}}(\text{NiS}) / [\text{Ni}^{2+}(\text{aq})] = (3 \times 10^{-19}) / (0.0100) = 3 \times 10^{-17} \text{ M}$$

Answer: **$3 \times 10^{-17} \text{ M}$**

If the CuS formed is filtered off before any NiS precipitates, how pure will the NiS precipitate be?

From above, NiS precipitates when $[\text{S}^{2-}(\text{aq})] = 3 \times 10^{-17} \text{ M}$. At this concentration,

$$[\text{Cu}^{2+}(\text{aq})] = K_{\text{sp}}(\text{CuS}) / [\text{S}^{2-}(\text{aq})] = (8 \times 10^{-34}) / (3 \times 10^{-17}) = 3 \times 10^{-17} \text{ M}$$

When NiS starts to precipitate, $[\text{Ni}^{2+}(\text{aq})] = 0.0100 \text{ M}$ and $[\text{Cu}^{2+}(\text{aq})] = 3 \times 10^{-17} \text{ M}$.

The NiS that precipitates will contain *very little* Cu^{2+} : it will be *very pure*.

Answer: **100%**