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• Consider the following half-reactions and their standard reduction potentials.

$$2\text{ClO}_{3^{-}} + 12\text{H}^{+} + 10\text{e}^{-} \rightarrow \text{Cl}_{2} + 6\text{H}_{2}\text{O} \qquad E^{\circ} = 1.47 \text{ V}$$
$$\text{S}_{2}\text{O}_{8}^{2^{-}} + 2\text{e}^{-} \rightarrow 2\text{SO}_{4}^{2^{-}} \qquad E^{\circ} = 2.01 \text{ V}$$

Give the overall cell reaction.

The half cell with the least positive reduction potential is reversed:

$$Cl_2 + 6H_2O + 5S_2O_8^{2-} \rightarrow 2ClO_3^{-} + 12H^+ + 10SO_4^{2-}$$

Calculate ΔG° and hence the value of K_c for the cell reaction at 298 K.

As the ClO_3^- / Cl_2 half cell is reversed, the standard cell potential is:

$$E^{0} = ((2.01) + (-1.47) \text{ V} = 0.54 \text{ V}$$

Using $\Delta G^{\circ} = -nFE^{\circ}$, the free energy change for this 10e⁻ process is:

$$\Delta G^{0} = -(10) \times (96485 \text{ C mol}^{-1}) \times (0.54 \text{ V}) = -521000 \text{ J mol}^{-1} = -521 \text{ kJ mol}^{-1}$$

Using $\Delta G^{\circ} = -RT \ln K_c$, the equilibrium constant is given by:

$$-521000 \text{ kJ mol}^{-1} = -(8.314 \text{ J K}^{-1} \text{ mol}^{-1} \times 298 \text{ K}) \times \ln K_c$$
 so $K_c = 2.14 \times 10^{90}$

Alternatively, K_c can be obtained directly from E^0 using the Nernst equation:

$$E^{0} = \frac{RT}{nF} \ln K_{c} = 0.54 \text{ V}$$

0.54 V = $\frac{(8.314 \text{ J K}^{-1} \text{ mol}^{-1} \times 298 \text{ K})}{(10 \times 96485 \text{ C mol}^{-1})} \ln K_{c}$ so $K_{c} = 2.14 \times 10^{90}$

The reaction essentially proceeds to completion.

$\Delta G^{\circ} = -521 \text{ kJ mol}^{-1}$	$K_{\rm c} = 2.14 \times 10^{90}$
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