- 3
- A bar of hot iron with a mass of 1.000 kg and a temperature of 100.00 °C is plunged into an insulated tank of water. The mass of water was 2.000 kg and its initial temperature was 25.00 °C. What will the temperature of the resulting system be when it has stabilised? (The specific heat capacities of water and iron are 4.184 J g⁻¹ K⁻¹ and 0.4498 J g⁻¹ K⁻¹, respectively.)

The heat lost by the iron is equal to the heat gained by the water.

The heat change is related to the temperature change through $q = mC\Delta T$ where *m* is the mass of the substance and *C* is its specific heat capacity.

For the water,

$$q = m_{\rm H_20} C_{\rm H_20} \Delta T_{\rm H_20} = (2.000 \times 10^3 \text{ g}) \times (4.184 \text{ J g}^{-1} \text{ K}^{-1}) \times ((T_{\rm f} - 25.00) \text{ K}) \\ = (8.368 \times 10^3 \text{ J K}^{-1}) \times ((T_{\rm f} - 25.00) \text{ K})$$

For the iron,

$$q = m_{\rm Fe} C_{\rm Fe} \Delta T_{\rm Fe} = (1.000 \times 10^3 \text{ g}) \times (0.4498 \text{ J g}^{-1}) \times ((T_{\rm f} - 100.00) \text{ K})$$
$$= (0.4498 \times 10^3 \text{ J K}^{-1}) \times ((T_{\rm f} - 100.00) \text{ K})$$

Hence, as $q_{water} = -q_{iron}$:

$$(8.368 \times 10^3 \text{ J K}^{-1}) \times ((T_f - 25.00) \text{ K}) = -(0.4498 \times 10^3 \text{ J K}^{-1}) \times ((T_f - 100.00) \text{ K})$$

 $T_{\rm f} = 28.83 \ ^{\circ}{\rm C}$

Answer: 28.83 °C