

- An aqueous solution with a volume of 10.0 mL contains 0.025 g of a purified protein of unknown molecular weight. The osmotic pressure of the solution was measured in an osmometer to be 0.0036 atm at 20.0 °C. Assuming ideal behaviour and no dissociation of the protein, estimate its molar mass.

The osmotic pressure is given by

$$\Pi = cRT$$

As 1 atm = 1.013×10^5 Pa, the osmotic pressure is

$$\Pi = (0.0036 \times 1.013 \times 10^5) \text{ Pa} = 365 \text{ Pa}$$

Hence

$$c = \Pi / RT = (365 \text{ Pa}) / ((8.314 \text{ m}^3 \text{ Pa K}^{-1} \text{ mol}^{-1}) \times (293 \text{ K})) = 0.15 \text{ mol m}^{-3}$$

As $1 \text{ m}^3 = 1000 \text{ L}$, this corresponds to

$$c = 1.5 \times 10^{-4} \text{ mol L}^{-1}$$

As 1 L contains 1.5×10^{-4} mol, the amount in 10.0 mL is:

$$\text{amount of protein} = (0.0100 \text{ L}) \times (1.5 \times 10^{-4} \text{ mol L}^{-1}) = 1.5 \times 10^{-6} \text{ mol}$$

As this amount has a mass of 0.025 g, the mass of 1 mol is:

$$\begin{aligned} \text{molar mass} &= \text{mass} / \text{number of moles} \\ &= (0.025 \text{ g}) / (1.5 \times 10^{-6} \text{ mol}) = 17000 \text{ g mol}^{-1} \end{aligned}$$

Answer: $1.7 \times 10^4 \text{ g mol}^{-1}$