Marks • Explain why a sustained fission chain reaction can only occur when a critical mass is prepared.

Below the critical mass, so many neutrons are lost from the material that a chain reaction cannot be sustained.

• The half life of <sup>3</sup>H is 12 years. Calculate how long it takes (rounded to the nearest year) for the activity of a sample of tritium to have dropped to 0.1% of its original value.

From 
$$t_{1/2} = \frac{\ln 2}{\lambda}$$
, the activity coefficient  $\lambda = \frac{\ln 2}{t_{1/2}} = \frac{\ln 2}{12 \text{ years}} = 0.058 \text{ years}^{-1}$ 

As the activity is directly proportional to the number of radioactive nuclei, the activity,  $A_t$ , at time *t* is related to the initial activity,  $A_0$ , by  $\ln\left(\frac{A_0}{A_1}\right) = \lambda t$ 

With 
$$A_t = 0.001 \times A_o$$
, the ratio  $\frac{A_0}{A_t} = 1000$ . Hence,

 $\ln(1000) = (0.058)t$  or t = 120 years  $= 1.2 \times 10^2$  years

Answer: 
$$1.2 \times 10^2$$
 years

• Consider the following list of unstable isotopes and their decay mechanisms.

 $^{33}_{17}\text{Cl} \rightarrow ^{0}_{+1}\text{e} + ^{33}_{16}\text{S}$ half-life = 2.5 s $^{32}_{15}P \rightarrow ^{0}_{-1}e + ^{32}_{16}S$ half-life = 14.3 days  $^{199}_{82}$ Pb  $\rightarrow ^{0}_{+1}$ e +  $^{199}_{81}$ Tl half-life = 90 minutes  $^{13}_{7}N \rightarrow ^{0}_{+1}e + ^{13}_{6}C$ half-life = 10 minutes

From this list, select the isotope that best satisfies the following requirements. Provide a reason for your choice in each case.

Requirement	Isotope	Reason for choice
Isotope used in medical imaging	<sup>13</sup> <sub>7</sub> N	Positron emitter, non-toxic and has sufficiently long half life to be chemically incorporated.
Decay represents the transformation of a neutron into a proton	<sup>32</sup> <sub>15</sub> P	This nuclide is a $\beta$ -emitter. The nuclear charge increases from 15 to 16 and the mass is unaffected. The charge is conserved by the emission of an electron.
The isotope with the highest molar activity	<sup>35</sup> 17Cl	It has the shortest half-life and, as $\lambda = \frac{\ln 2}{t_{1/2}}$ . it therefore has the highest activity.

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