

Explain in terms of bond order why the upper state of the violet system exhibits a shorter bond length (1.15 Å) than the ground state (1.17 Å).

**The bond order is an indication of the bond strength and bond length. A higher bond order leads to a strong and shorter bond. It can be calculated as:**

$$\text{bond order} = \frac{1}{2} (\text{number of bonding electrons} - \text{number of antibonding electrons})$$

**The upper state in the violet system has 8 bonding electrons ( $2 \times \sigma$ ,  $4 \times \sigma^*$  and  $2 \times \sigma$ ) and 1 antibonding electron ( $1 \times \sigma^*$ ):**

$$\text{bond order} = \frac{1}{2} (8 - 1) = 7/2$$

**The upper state in the red system has 7 bonding electrons ( $2 \times \sigma$ ,  $3 \times \sigma^*$  and  $2 \times \sigma$ ) and 2 antibonding electron ( $2 \times \sigma^*$ ):**

$$\text{bond order} = \frac{1}{2} (7 - 2) = 5/2$$

**The upper state in the violet system has a higher bond order and this is consistent with it having a shorter bond (i.e. it has more bonding and fewer antibonding electrons).**

Also indicated in Huggin's spectrum are the Fraunhofer absorption features labelled K, H and G, which arise from calcium. Explain the appearance of these features. (Hint: they would also appear in the spectrum of moonlight.)

**Blackbody emission from the sun is absorbed by Ca in the sun's atmosphere. the solar spectrum is then reflected by the comet.**

The Fraunhofer feature labelled 'h' is due to atomic hydrogen. What is the electronic transition responsible for this absorption feature? (Hint: one of the energy levels involved is  $n = 2$ .)

**The feature occurs at 41 nm. This corresponds to an energy of:**

$$E = (hc/\lambda) = (6.626 \times 10^{-34} \text{ J s} \times 2.998 \times 10^8 \text{ m s}^{-1}) / (41 \times 10^{-8} \text{ m}) = 4.85 \times 10^{-19} \text{ J}$$

**The energy of a level in hydrogen is given by  $E_n = -E_R(1/n^2)$ . The transition energy is the difference in the energies of the two levels involved:**

$$\Delta E = \frac{-E_R}{n_f^2} - \frac{-E_R}{n_i^2} = E_R \left[ \frac{1}{n_i^2} - \frac{1}{n_f^2} \right] \text{ where } E_R \text{ is the Rydberg constant.}$$

As  $n_i = 2$ ,

$$\Delta E = (2.18 \times 10^{-18} \text{ J}) \left[ \frac{1}{2^2} - \frac{1}{n_f^2} \right] = 4.85 \times 10^{-19} \text{ J} \text{ which gives } n_f = 6.$$