Marks

• Oxalic acid,  $H_2C_2O_4$ , found in rhubarb, causes muscle spasms by precipitating  $Ca^{2+}$  ions from the blood as calcium oxalate,  $CaC_2O_4$ ·H<sub>2</sub>O. Given the solubility product constant for calcium oxalate is  $2.3 \times 10^{-9}$  M<sup>2</sup>, calculate the concentration of calcium ions in g L<sup>-1</sup> formed by dissolving CaC<sub>2</sub>O<sub>4</sub>·H<sub>2</sub>O in water at 25 °C to give a saturated solution.

The dissolution equilibrium for CaC<sub>2</sub>O<sub>4</sub>.H<sub>2</sub>O is:

$$CaC_2O_4.H_2O(s) \iff Ca^{2+}(aq) + C_2O_4^{2-}(aq) + H_2O(l)$$

Hence, the solubility product  $K_{sp} = [Ca^{2+}(aq)][C_2O_4^{2-}(aq)]$ 

The chemical equation shows that dissolution of one mole of  $CaC_2O_4$ . $H_2O(s)$  leads to one mole of  $Ca^{2+}(aq)$  and one mole of  $C_2O_4^{2-}(aq)$ .

If 
$$[Ca^{2+}(aq)] = [C_2O_4^{2-}(aq)] = x$$
,  
 $K_{sp} = x^2 = 2.3 \times 10^{-9}$  so  $x = 4.8 \times 10^{-5}$ 

 $Ca^{2+}$  will be present at 4.8 × 10<sup>-5</sup> mol L<sup>-1</sup>. As the atomic mass of Ca is 40.08, this corresponds to a mass of:

mass of  $Ca^{2+}$  ions = number of moles × atomic mass =  $(4.8 \times 10^{-5}) \times 40.08 = 1.9 \times 10^{-3} \text{ g}$ 

Answer:  $1.9 \times 10^{-3}$  g

• The following initial rate data have been obtained for the gas phase reaction of nitrogen dioxide,  $NO_2(g)$ , and ozone,  $O_3(g)$ , at 300 K.

$2NO_2(g) + O_3(g) \rightarrow N_2O_5(g) + O_2(g)$						
[NO <sub>2</sub> (g)] M	[O <sub>3</sub> (g)] M	Rate M s <sup>-1</sup>				
0.65	0.80	$2.61 \times 10^4$				
1.10	0.80	$4.40 \times 10^{4}$				
1.10	1.60	$8.80 \times 10^{4}$				

 $2NO_{2}(\alpha) + O_{2}(\alpha) \rightarrow N_{2}O_{2}(\alpha) + O_{2}(\alpha)$ 

What is the order of this reaction with respect to each reagent?

Between the first and second experiments,  $[O_3(g)]$  is kept constant and  $[NO_2(g)]$ increases by about 1.7. This leads to the rate also increasing by about 1.7. The reaction is therefore first order with respect to [NO<sub>2</sub>(g)].

Between the second and third experiments,  $[NO_2(g)]$  is kept constant and  $[O_3(g)]$ is doubled. This also leads to a doubling of the rate. The reaction is therefore also first order with respect to  $[O_3(g)]$ .

rate =  $k[NO_2(g)][O_3(g)]$ 

What is the rate constant of the reaction?

Using the rate law rate =  $k[NO_2(g)][O_3(g)]$ , k can be worked out using any of the three experiments. For example, using the first experiment:

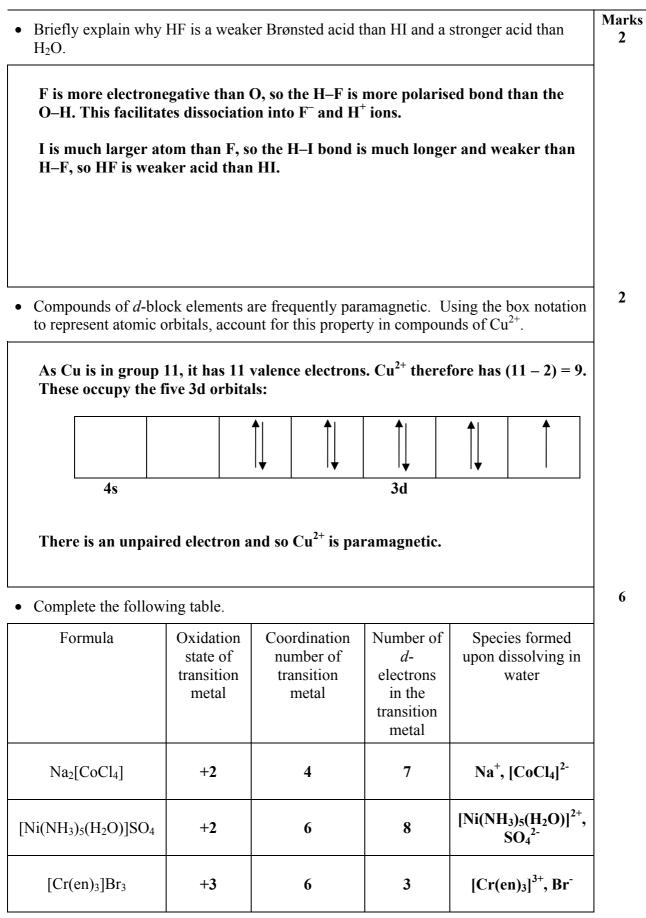
rate =  $2.61 \times 10^4$  = k[NO<sub>2</sub>(g)][O<sub>3</sub>(g)] = k × (0.65) × (0.80)

Hence k =  $\frac{2.61 \times 10^4}{(0.65)(0.80)} = 5.0 \times 10^4$ 

The units of k are obtained by balancing those in the rate law: the rate has units of M s<sup>-1</sup> and the concentrations both have units of M. Hence:

Units of k = 
$$\frac{M s^{-1}}{(M)(M)} = M^{-1} s^{-1}$$

Answer:  $5.0 \times 10^4 \text{ M}^{-1} \text{ s}^{-1}$ 



 $en = ethylenediamine = NH_2CH_2CH_2NH_2$ 

• Solution A consists of a 0.25 M aqueous solution of hydrazoic acid, HN<sub>3</sub>, at 25 °C. Calculate the pH of Solution A. The  $pK_a$  of HN<sub>3</sub> is 4.63.

## As $pK_a = -log(K_a) = 4.63$ , $K_a = 10^{-4.63} = 2.34 \times 10^{-5}$ . The reaction table is:

	HN <sub>3</sub> (aq)	<b>~</b>	H <sup>+</sup> (aq)	N <sub>3</sub> (aq)
t = 0	0.25		0	0
change	-X		+ <b>x</b>	+x
equilibrium	0.25 - x		X	X

Hence, 
$$K_a = \frac{[H^+(aq)][N_3^-(aq)]}{[HN_3]} = \frac{(x)(x)}{(0.25-x)} = \frac{x^2}{(0.25-x)} = 2.34 \times 10^{-5}$$

As  $K_a$  is very small, very little HN<sub>3</sub> dissociates and x is tiny so  $(0.25 - x) \sim 0.25$ 

Hence, 
$$\frac{x^2}{(0.25)} = 2.34 \times 10^{-5}$$
 or  $x = [H^+(aq)] = 2.42 \times 10^{-3} M$ 

As  $pH = -log[H^+(aq)]$ :

 $pH = -log(2.42 \times 10^{-3}) = 2.62$ 

Answer: 2.62

## (ANSWER CONTINUES ON THE NEXT PAGE)

At 25 °C, 1.00 L of Solution B consists of 13.0 g of sodium azide  $(NaN_3)$  dissolved in water. Calculate the pH of Solution B.

The relevant reaction is now:  $N_3(aq) + H_2O(l) \iff HN_3(aq) + OH(aq)$ 

As  $N_3$  is the conjugate base of HN<sub>3</sub>, the equilibrium constant for this reaction is  $K_b$  where  $pK_a + pK_b = 14.00$ .

Hence, using pK<sub>a</sub> from above:

 $pK_b = 14.00 - 4.63 = 9.37$  or  $K_b = 10^{-9.37} = 4.27 \times 10^{-10}$ .

The molar mass of NaN<sub>3</sub> is  $(22.99 (Na)) + (3 \times 14.01 (N)) = 65.02$ . The number of moles in 13.0 g is therefore:

number of moles =  $\frac{\text{mass}}{\text{molar mass}} = \frac{13.0}{65.02} = 0.200 \text{ mol}$ 

As this is dissolved in 1.00 L,  $[N_3(aq)] = \frac{\text{number of moles}}{\text{volume}} = \frac{0.200}{1.00} = 0.200 \text{ M}$ 

The relevant reaction table is now:

	N <sub>3</sub> (aq)	H <sub>2</sub> O(l)	<b>_</b>	HN <sub>3</sub> (aq)	OH <sup>-</sup> (aq)
t = 0	0.200			0	0
change	-X			+ <b>x</b>	+ <b>x</b>
equilibrium	0.200 - x			X	X

The equilibrium constant  $K_b = \frac{[NH_3(aq)][OH^-(aq)]}{[N_3^-(aq)]} = \frac{(x)(x)}{(0.200-x)} = \frac{x^2}{(0.200-x)}$ 

 $K_b$  is small so the amount of  $N_3^-(aq)$  which is protonated is tiny and hence  $0.200-x\sim 0.200.$ 

Hence,  $\frac{x^2}{(0.200)} = 4.27 \times 10^{-10}$  or  $x = [OH^{-}(aq)] = 9.24 \times 10^{-6} M$ As  $pOH = -log[OH(aq)] = -log(9.24 \times 10^{-6}) = 5.03$ As pH + pOH = 14: pH = 14 - 5.03 = 8.97

Answer: 8.97

## 2006-N-5

Solution B (1.00 L) is poured into Solution A (1.00 L) and allowed to equilibrate at 25  $^{\circ}$ C to give Solution C. Calculate the pH of Solution C.

Solution C is a buffer system as it contains both a weak acid  $(HN_3)$  and its conjugate base  $(N_3(aq))$ . The pH can be obtained from the Henderson-Hasselbalch equation:

$$pH = pK_a + log \frac{[A^{-}(aq)]}{[HA(aq)]}$$

Using  $pK_a = 4.63$ ,  $[HA(aq)] = [HN_3(aq)] = 0.25$  M and  $[A^-(aq)] = [N_3^-(aq)] = 0.200$  M:

$$pH = (4.63) + \log \frac{(0.200)}{(0.25)} = 4.53$$

Answer: 4.53

If you wanted to adjust the pH of Solution C to be exactly equal to 4.00, which component in the mixture would you need to increase in concentration? To lower the pH, the acid concentration (HN<sub>3</sub>) is increased Define what is meant by an "allotrope". Give an example of a pair of allotropes 3
Allotropes are different structural forms of the same element.
Examples include diamond and graphite for carbon; red and white phosphorus; oxygen O<sub>2</sub> and ozone O<sub>3</sub>.

