

1. (a) Between experiments (1) and (2), [NO] is constant. Doubling [O<sub>2</sub>] leads to the initial reaction rate doubling:

the reaction is first order with respect to O<sub>2</sub>.

Between experiments (1) and (3), [O<sub>2</sub>] is constant. Doubling [NO] leads to the initial reaction rate increases by a factor of four:

the reaction is second order with respect to NO.

Thus,

$$\text{rate} \propto [\text{O}_2][\text{NO}]^2 = k[\text{O}_2][\text{NO}]^2$$

Using experiment (1), rate =  $3.20 \times 10^{-3} \text{ mol L}^{-1} \text{ s}^{-1}$  when  $[\text{O}_2] = 1.10 \times 10^{-2} \text{ mol L}^{-1}$  and  $[\text{NO}] = 1.30 \times 10^{-2} \text{ mol L}^{-1}$ . Hence, for  $k$  and its units:

$$3.20 \times 10^{-3} \text{ mol L}^{-1} \text{ s}^{-1} = k \times (1.10 \times 10^{-2} \text{ mol L}^{-1}) \times (1.30 \times 10^{-2} \text{ mol L}^{-1})^2$$

$$(\text{mol L}^{-1} \text{ s}^{-1}) = (\text{units of } k) \times (\text{mol L}^{-1}) \times (\text{mol L}^{-1})^2$$

$$k = 1.7 \times 10^3 \text{ mol}^{-2} \text{ L}^2 \text{ s}^{-1}$$

- (b) According to the reaction equation:



Two moles of NO<sub>2</sub> are produced for every mole of O<sub>2</sub> which reacts. The react of formation of NO<sub>2</sub> is thus twice the rate of consumption of oxygen. If the initial rate of consumption of oxygen is  $1 \times 10^3 \text{ mol L}^{-1} \text{ s}^{-1}$ , the initial rate of formation of NO<sub>2</sub>(g) is  $2 \times 10^3 \text{ mol L}^{-1} \text{ s}^{-1}$ .

2. For a first order reaction, the rate constant and half life are related by  $k = \frac{\ln 2}{t_{1/2}}$ .

Thus,

$$k = \frac{\ln 2}{(6.00 \times 10^4 \text{ s})} = 1.16 \times 10^{-5} \text{ s}^{-1}$$

3. The rate constants at two different temperatures are related through the Arrhenius equation:

$$\ln\left(\frac{k_2}{k_1}\right) = \frac{E_a}{R} \left(\frac{1}{T_1} - \frac{1}{T_2}\right)$$

Thus,

$$\ln \left( \frac{0.248 \text{ L mol}^{-1} \text{ s}^{-1}}{0.208 \text{ L mol}^{-1} \text{ s}^{-1}} \right) = \frac{E_a}{(8.314 \text{ J K}^{-1} \text{ mol}^{-1})} \left( \frac{1}{(37 + 273) \text{ K}} - \frac{1}{(40 + 273) \text{ K}} \right)$$

$$E_a = 47300 \text{ J mol}^{-1} = 47.3 \text{ kJ mol}^{-1}$$

The “*A*” factor can be determined using *k* and *E<sub>a</sub>* at either temperature using the Arrhenius equation:

$$k = A e^{-E_a/RT}$$

At *T* = 37 °C, *k* = 0.208 mol<sup>-1</sup> L s<sup>-1</sup>,

$$0.208 \text{ mol L}^{-1} \text{ s}^{-1} = A \times (e^{-47300/(8.314 \times (37 + 273))})$$

$$A = 1.94 \times 10^7 \text{ mol}^{-1} \text{ L s}^{-1} \quad (\text{note that “}A\text{” has the same units as }k)$$

4. (a) As the second reaction is slow, it is rate determining. From the mechanism, the rate of this step is given by:

$$\text{rate} = k_2[\text{O}_3][\text{O}]$$

As *O* is a highly reactive intermediate, its concentration cannot be included in the rate equation which is to be experimentally tested. As the first step is fast, the equilibrium between *O*<sub>3</sub> and *O*<sub>2</sub> + *O* will be set up rapidly and maintained for most of the reaction. For an equilibrium,

$$\text{rate forward reaction} = \text{rate backward reaction}$$

$$k_1[\text{O}_3] = k_{-1}[\text{O}_2][\text{O}] \text{ or } [\text{O}] = \frac{k_1}{k_{-1}} \frac{[\text{O}_3]}{[\text{O}_2]}$$

Hence,

$$\begin{aligned} \text{rate} &= k_2[\text{O}_3][\text{O}] \\ &= k_2[\text{O}_3] \times \frac{k_1}{k_{-1}} \frac{[\text{O}_3]}{[\text{O}_2]} = \frac{k_1 k_2}{k_{-1}} \frac{[\text{O}_3]^2}{[\text{O}_2]} = k \frac{[\text{O}_3]^2}{[\text{O}_2]} \text{ where } k = \frac{k_1 k_2}{k_{-1}} \end{aligned}$$

- (b) The rate determining step (step 2) involves the reaction of one molecule of *O*<sub>2</sub> with one atom of *O*. The molecularity is thus two: a bimolecular reaction.