CHEM1612 Answers to Problem Sheet 7

- 1. (a) HNO<sub>3</sub> is a very strong acid so the NO<sub>3</sub> (aq) ion is not basic. A solution of KNO<sub>3</sub> contains  $K^+(aq)$  and NO<sub>3</sub> (aq) ions and is neutral.
  - (b) FeCl<sub>3</sub> dissolves to give  $Fe^{3+}(aq)$  and 3CI(aq) ions. The small and high charged  $Fe^{3+}$  ion is surrounded by six water molecules in aqueous solution and acts as a weak acid because of the equilibrium:

$$[Fe(H_2O)_6]^{3+}(aq) + H_2O(l) \iff [Fe(H_2O)_5(OH)]^{2+}(aq) + H_3O^{+}(l)$$

The Cl<sup> $\cdot$ </sup> ion, the anion of a strong acid HCl, does not react and stays in solution as Cl<sup> $\cdot$ </sup>(aq). The solution is therefore acidic.

- (c)  $Ca(OH)_2$  is a strong base and dissolves to give  $Ca^{2+}(aq)$  and OH'(aq) ions. A solution of  $Ca(OH)_2$  is thus basic.
- (d)  $(NH_4)_2SO_4$  dissolves to give  $SO_4^{2-}(aq)$ , the anion of a strong acid,  $H_2SO_4$ , and  $NH_4^+$ , the cation of a weak base,  $NH_3$ .  $SO_4^{2-}(aq)$  does not react but  $NH_4^+$  is a weak acid and the solution is acidic because of the equilibrium:

$$NH_4^+(aq) + H_2O(l) \iff NH_3(aq) + H_3O^+(l)$$

(e) NaN<sub>3</sub> dissolves to give Na<sup>+</sup>(aq) and N<sub>3</sub><sup>-</sup>(aq), the anion of a weak acid. This anion is thus a weak base and the solution is basic because of the equilibrium:

$$N_3^{-}(aq) + H_2O(l) \iff HN_3(aq) + OH^{-}(aq)$$

- (f) BaCl<sub>2</sub> dissolves to give  $Ba^{2+}(aq)$  and 2Cl<sup>-</sup>(aq) ions. HCl is a very strong acid so the Cl<sup>-</sup>(aq) ion is not basic. The  $Ba^{2+}$  ion is large and is not acidic.
- 2. The solubility equilibrium is:

$$Ca_3(PO_4)_2(s) \implies 3Ca^{2+}(aq) + 2PO_4^{3-}(aq)$$

for which the solubility product is:

 $K_{\rm sp} = [{\rm Ca}^{2+}({\rm aq})]^3 [{\rm PO}_4^{2-}({\rm aq})]^2$ 

(a) If the molar solubility is equal to S then, from the equilibrium equation,  $[Ca^{2+}(aq)] = 3S$  and  $[PO_4^{3-}(aq)] = 2S$  and the solubility product becomes:

$$K_{\rm sp} = [{\rm Ca}^{2+}({\rm aq})]^3 [{\rm PO}_4^{3-}({\rm aq})]^2 = (3S)^3 \times (2S)^2 = 108S^5 = 1.3 \times 10^{-32}$$

molar solubility =  $S = 1.6 \times 10^{-7}$  M

The molar mass of Ca<sub>3</sub>(PO<sub>4</sub>)<sub>2</sub> is:

 $(3 \times 40.08 (Ca)) + 2 \times (30.97 (P) + 4 \times 16.00 (O)) \text{ g mol}^{-1} = 310.18 \text{ g mol}^{-1}$ 

Therefore, the solubility in g  $L^{-1}$  is:

solubility = molar solubility × formula mass =  $(1.6 \times 10^7 \text{ mol } \text{L}^{-1}) \times (310.18 \text{ g mol}^{-1}) = 5.0 \times 10^{-3} \text{ g } \text{L}^{-1}$ 

(b) Na<sub>3</sub>PO<sub>4</sub> dissolves completely to give  $[PO_4^{3-}(aq)] = 0.20$  M. The amount of PO<sub>4</sub><sup>3-</sup>(aq) from Ca<sub>3</sub>(PO<sub>4</sub>)<sub>2</sub> is tiny in comparison to that from Na<sub>3</sub>PO<sub>4</sub>. Denoting the molar solubility by *S* again, *K*<sub>sp</sub> is, as above:

$$K_{\rm sp} = [{\rm Ca}^{2+}({\rm aq})]^3 [{\rm PO}_4^{3-}({\rm aq})]^2 = (3S)^3 \times ([{\rm PO}_4^{2-}({\rm aq})])^2$$
$$27S^3 \times (0.20)^2 = 1.3 \times 10^{-32} \text{ so molar solubility} = S = 2.3 \times 10^{-11} \text{ M}$$

3. The solubility equilibrium for  $Ag_2SO_4(s)$  is:

$$Ag_2SO_4(s)$$
)  $\Longrightarrow$   $2Ag^+(aq) + SO_4^{-2}(aq)$ 

for which the solubility product is:

$$K_{\rm sp} = [{\rm Ag}^+({\rm aq})]^2 [{\rm SO_4}^{2-}({\rm aq})] = 2 \times 10^{-5}$$

As  $[Ag^+] = 0.01$  M and  $[SO_4^{2-}(aq)] = 0.01$  M before mixing and equal volumes are mixed, the concentrations will halve:  $[Ag^+] = 0.005$  M and  $[SO_4^{2-}(aq)] = 0.005$  M the reaction quotient or *ionic product* is

$$Q_{\rm sp} = (0.005)^2 \times (0.005) = 1 \times 10^{-7}$$

As  $Q_{sp} < K_{sp}$ , the equilibrium will proceed to the right and the solid will dissolve – no precipitate will form.

4.	(a) K <u>Mn</u> O <sub>4</sub>	$K^{+} Mn^{7+} 4O^{2-}$	Mn is +7		
	(b) <u>S</u> O <sub>4</sub> <sup>2–</sup>	$S^{6+} 4O^{2-}$	S is +6		
	(c) Na <sub>2</sub> O <sub>2</sub>	2Na <sup>+</sup> 2O <sup>-</sup>	O is -1 (oxygen in a peroxide)		
	(d) M <u>gH</u> <sub>2</sub>	Mg <sup>2+</sup> 2H <sup>-</sup>	H is -1 (hydrogen as a hydride with a metal)		
	(e) $N\underline{H}_4^+$	$N^{3-} 4H^+$	H is +1 (hydrogen in combination with a non-metal)		
	(f) <u>Br</u> F <sub>3</sub>	Br <sup>3+</sup> 3F <sup>-</sup>	Br is +3		
	(g) [ <u>Ni</u> (NH <sub>3</sub> ) <sub>6</sub>	$[5]^{2+}$ Ni <sup>2+</sup> 6NH <sub>3</sub>	Ni is +2 (ammonia is a neutral ligand)		
	(h) K <sub>4</sub> [ <u>Fe</u> (CN	$()_6]$ <b>4K<sup>+</sup> Fe<sup>2+</sup> 6C</b>	<b>N</b> Fe is +2 (cyanide is an anionic ligand)		

5.  $K_{\text{stab}}$  refers to the equilibrium:

 $Zn^{2+}(aq) + 4NH_3(aq) \implies [Zn(NH_3)_4]^{2+}(aq)$ 

As  $K_{\text{stab}} = 8 \times 10^8$  and is *very* large, the reaction essentially goes to completion. The reaction requires a 4:1 ratio NH<sub>3</sub> :  $\text{Zn}^{2+}(\text{aq})$  ions and as 3.0 mol of NH<sub>3</sub> and 0.10 mol of Zn<sup>2+</sup>(aq) is present, NH<sub>3</sub> is in excess.

Let the tiny amount of  $Zn^{2+}(aq)$  and its concentration in 1.5 L after complexation be:

amount of  $Zn^{2+}(aq) = x$  mol and

$$[Zn^{2+}(aq)] = \frac{\text{number of moles}}{\text{volume}} = \frac{x}{1.5} \text{ M}$$

The amount of  $[Zn(NH_3)_4]^{2+}(aq)$  formed is therefore:

amount of 
$$[Zn(NH_3)_4]^{2+}(aq) = (0.10 - x) mol$$

As x is so small, this amount and hence the concentration can be approximated as:

amount of 
$$[Zn(NH_3)_4]^{2+}(aq) = (0.10 - x) \sim 0.10 \text{ mol}$$

$$[[Zn(NH_3)_4]^{2+}(aq)] \sim \frac{0.10}{1.5} M$$

Formation of 0.10 mol of  $[Zn(NH_3)_4]^{2+}(aq)$  requires 0.40 mol of ammonia, leaving:

amount of  $NH_3 = (3.0 - 4 \times 0.10) = 2.6$  mol and

$$[\mathrm{NH}_3(\mathrm{aq})] = \frac{2.6}{1.5} \mathrm{M}$$

Hence,

$$K_{\text{stab}} = \frac{\left[\left[\text{Zn}(\text{NH}_{3})_{4}\right]^{2+}(\text{aq})\right]}{\left[\text{Zn}^{2+}(\text{aq})\right]\left[\text{NH}_{3}(\text{aq})\right]^{4}} = \frac{\left(\frac{0.10}{1.5}\right)}{\left(\frac{x}{1.5}\right)\left(\frac{2.6}{1.5}\right)^{4}} = 8 \times 10^{8}$$
$$x = 1.4 \times 10^{-11} \text{ mol and } \left[\text{Zn}^{2+}(\text{aq})\right] = 9.2 \times 10^{-12} \text{ M}$$

6.

## (a) **100 mL of blood contains 15.0 g of haemoglobin corresponding to:**

number of moles of haemoglobin =  $\frac{\text{mass}}{\text{molar mass}} = \frac{15.0 \text{ g}}{6.45 \times 10^4 \text{ g mol}^{-1}}$ =  $2.33 \times 10^{-4} \text{ mol}$ 

As each haemoglobin can bind 4 molecules of O<sub>2</sub>:

number of moles of 
$$O_2 = 4 \times 2.33 \times 10^{-4}$$
 mol =  $9.30 \times 10^{-4}$  mol

As 101.3 kPa = 1 atm, using the ideal gas equation, PV = nRT, at 311 K and 101.3 kPa, this will occupy a volume of:

$$V = \frac{nRT}{P} = \frac{(9.30 \times 10^{-4} \text{ mol}) \times (0.08206 \text{ L atm K}^{-1} \text{ mol}^{-1}) \times (311 \text{ K})}{(1 \text{ atm})}$$
  
= 0.0237 L

(b) **1 kg of haemoglobin corresponds to:** 

number of moles of haemoglobin =  $\frac{1000 \text{ g}}{6.45 \times 10^4 \text{ g mol}^{-1}} = 0.0155 \text{ mol}$ 

3.4 g of iron corresponds to:

number of moles of iron 
$$= \frac{\text{mass}}{\text{atomic mass}} = \frac{3.4 \text{ g}}{55.85 \text{ g mol}^{-1}} = 0.061 \text{ mol}$$

Therefore, the number of iron atoms per haemoglobin is  $=\frac{0.061}{0.0155}=4$ 

Each iron atom binds one O2 molecule.

(c) Fe is in Group 8 so has 8 valence electrons with a configuration  $[Ar]4s^23d^6$ . Possible oxidation states include Fe<sup>+</sup>, Fe<sup>2+</sup>, Fe<sup>3+</sup>, Fe<sup>4+</sup> and Fe<sup>6+</sup>. As the 4s electrons are lost first, these oxidation states correspond to the following electron arrangments:

	<b>4</b> <i>s</i>			3 <i>d</i>			number of unpaired electrons
Fe	$\uparrow\downarrow$	$\uparrow\downarrow$	1	↑	1	$\uparrow$	4
$\mathbf{Fe}^+$	$\uparrow$	↑↓	↑	$\uparrow$	1	↑	5
Fe <sup>2+</sup>		↑↓	↑	↑	↑	↑	4
Fe <sup>3+</sup>		↑	↑	↑	$\uparrow$	$\uparrow$	5
Fe <sup>4+</sup>		↑	↑	↑	↑		4
Fe <sup>6+</sup>		$\uparrow$	$\uparrow$				2

The magnetic studies are consistent with an  $Fe^{2+}$  or an  $Fe^{4+}$  being present.  $Fe^{2+}$  is much more common and it is this oxidation state which is actually present in haemoglobin.