### Topics in the November 2008 Exam Paper for CHEM1612

Click on the links for resources on each topic.

2008-N-2:

• Introduction to Chemical Energetics

2008-N-3:

• Introduction to Chemical Energetics

2008-N-4:

Solutions

### 2008-N-5:

Chemical Equilibrium

2008-N-6:

• Chemical Equilibrium

2008-N-7:

• Acids and Bases

### 2008-N-8:

• Complexes

### 2008-N-9:

• Redox Reactions and Introduction to Electrochemistry

2008-N-10:

- Radiochemistry
- Solubility

### 2008-N-11:

- Introduction to Colloids and Surface Chemistry
- Redox Reactions and Introduction to Electrochemistry

2008-N-12:

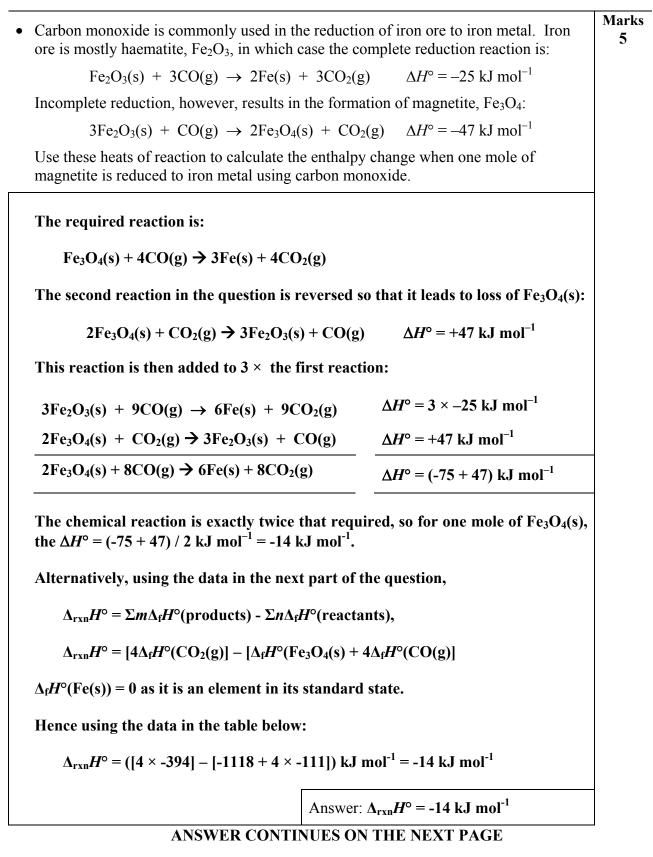
• Chemical Kinetics

#### 2008-N-13:

Redox Reactions and Introduction to Electrochemistry

2008-N-14:

- Chemical Kinetics
- Introduction to Colloids and Surface Chemistry



- Marks
  - 2
- A concentration cell containing aqueous solutions of Cu(NO<sub>3</sub>)<sub>2</sub> and solid copper metal is constructed so that the Cu<sup>2+</sup> ion concentration in the cathode half-cell is 0.66 M. Calculate the concentration of the Cu<sup>2+</sup> ion in the anode half-cell if the cell potential for the concentration cell at 25 °C is 0.03 V.

The cathode and anode reactions are:  $Cu^{2+}(aq) + 2e^{-} \Rightarrow Cu(s) \quad (cathode)$   $Cu(s) \Rightarrow Cu^{2+}(aq) + 2e^{-} \quad (anode)$ The standard electrode potential  $E^{\circ} = 0$  V and the potential can be calculated using the Nernst equation for this 2 electron reaction, n = 2:  $E = E^{\circ} - \frac{RT}{nF} \ln Q = -\frac{RT}{nF} \ln \left( \frac{[Cu^{2+}(aq)]_{anode}}{[Cu^{2+}(aq)]_{anode}} \right)$   $= -\frac{(8.314 \text{ J K}^{-1} \text{ mol}^{-1})(298 \text{ K})}{(2 \times 96485 \text{ C mol}^{-1})} \ln \left( \frac{[Cu^{2+}(aq)]_{anode}}{0.66} \right) = +0.03 \text{ V}$ This gives  $[Cu^{2+}(aq)]_{anode} = 0.06 \text{ M}.$ 

• In **acid solution**, dichromate ion oxidises iron(II) to iron(III) as illustrated in the partial equation:

 $Fe^{2+} + Cr_2O_7^{2-} \rightarrow Fe^{3+} + Cr^{3+}$ 

Answer: 0.06 M

Write a balanced equation for this reaction.

The half reactions are:

$$Fe^{2^+} \rightarrow Fe^{3^+} + e^-$$
  
 $Cr_2O_7^{2^-} + 14H^+ + 6e^- \rightarrow 2Cr^{3^+} + 7H_2O$ 

where  $H^+$  has been added to the  $Cr_2O_7^{2-}/Cr^{3+}$  couple to give  $H_2O$ .

To balance the electrons, the first reaction needs to be multiplied by 6. Hence:

$$6Fe^{2+} + Cr_2O_7^{2-} + 14H^+ \rightarrow 6Fe^{3+} + 2Cr^{3+} + 7H_2O$$

What would happen to the cell potential if the concentration of  $Cr^{3+}$  were increased?

It would decrease. If [Cr<sup>3+</sup>] is increased, Le Châtelier's principle predicts that the reaction will shift towards reactants, reducing the cell potential.

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Another iron oxide that can be formed as an intermediate during reduction is FeO. Use the following table of thermochemical data to show whether the formation of FeO from  $Fe_3O_4$  is spontaneous or not at 25 °C.

	$\Delta_{\rm f} H^{\circ}  ({\rm kJ}  {\rm mol}^{-1})$	$S^{\circ}$ (J K <sup>-1</sup> mol <sup>-1</sup> )
FeO	-272	61
Fe <sub>3</sub> O <sub>4</sub>	-1118	146
СО	-111	198
CO <sub>2</sub>	-394	214

For the reaction,

 $Fe_3O_4(s) + CO(g) \rightarrow 3FeO(s) + CO_2(g)$ 

$$\Delta_{rxn} H^{\circ} = \Sigma m \Delta_{f} H^{\circ} (\text{products}) - \Sigma n \Delta_{f} H^{\circ} (\text{reactants})$$
  
= ([3 × -272 -394] - [-1118 - 111]) kJ mol<sup>-1</sup> = +19 kJ mol<sup>-1</sup>

$$\Delta_{rxn}S^{\circ} = \Sigma mS^{\circ}(\text{products}) - \Sigma nS^{\circ}(\text{reactants})$$
  
= ([3 × 61 + 214] - [146 + 146]) J K<sup>-1</sup> mol<sup>-1</sup> = +53 J K<sup>-1</sup> mol<sup>-1</sup>

Thus,

$$\Delta_{rxn}G^{\circ} = \Delta_{rxn}H^{\circ} - T\Delta_{rxn}S^{\circ}$$
  
= (+19 × 10<sup>3</sup> J mol<sup>-1</sup>) – (298 K)(53 J K<sup>-1</sup> mol<sup>-1</sup>)  
= +3200 J mol<sup>-1</sup> = +3.2 kJ mol<sup>-1</sup>

As  $\Delta_{rxn} G^{\circ} > 0$ , the reaction is not spontaneous.

Marks • A 150.0 g block of iron metal is cooled by placing it in an insulated container with 4 a 50.0 g block of ice at 0.0 °C. The ice melts, and when the system comes to equilibrium the temperature of the water is 78.0 °C. What was the original temperature (in °C) of the iron? The specific heat capacity of liquid water is  $4.184 \text{ J K}^{-1} \text{ g}^{-1}$ . Data: The specific heat capacity of solid iron is  $0.450 \text{ J K}^{-1} \text{ g}^{-1}$ . The molar enthalpy of fusion of ice (water) is  $6.007 \text{ kJ mol}^{-1}$ . The heat from the iron is used to melt the ice and to warm the water from 0.0 °C to 78.0 °C. The molar mass of H<sub>2</sub>O is  $(2 \times 1.008 \text{ (H)} + 16.00 \text{ (O)}) \text{ g mol}^{-1} = 18.02 \text{ g mol}^{-1}$ . Hence 50.0 g of ice corresponds to: number of moles = mass / molar mass =  $(50.0 \text{ g}) / (18.02 \text{ g mol}^{-1}) = 2.775 \text{ mol}.$ Hence the heat used to melt ice is:  $q_1 = 6.007 \text{ kJ mol}^{-1} \times 2.775 \text{ mol} = 16.67 \text{ kJ} = 16670 \text{ J}$ The heat used to warm 50.0 g water by 78.0 °C is:  $q_2 = m \times C \times \Delta T = (50.0 \text{ g}) \times (4.184 \text{ J K}^{-1} \text{ g}^{-1}) \times (78.0 \text{ K}) = 16320 \text{ J}$ Overall, the heat transferred from the iron is:  $q = q_1 + q_2 = 16670 \text{ J} + 16320 \text{ J} = 32990 \text{ J}$ This heat is lost from 150.0 g of iron leading to it cooling by  $\Delta T$ :  $q = m \times C \times \Delta T = (150.0 \text{ g}) \times (0.450 \text{ J K}^{-1} \text{ g}^{-1}) \times \Delta T = 32990 \text{ J}$  $\Delta T = 489 \text{ K} = 489 \text{ }^{\circ}\text{C}$ As the final temperature of the iron is 78.0 °C, its original temperature was (78.0 + 489) °C = 567 °C. Answer: 567 °C

- Marks 5
- The freezing point of a sample of seawater is measured as -2.15 °C at 1 atm pressure. Assuming that the concentrations of other solutes are negligible, and that the salt does not significantly change the density of the water from  $1.00 \text{ kg L}^{-1}$ , determine the concentration (in mol  $L^{-1}$ ) of NaCl in this sample. (The molal freezing point depression constant for H<sub>2</sub>O is 1.86 °C m<sup>-1</sup>) The freezing point depression,  $\Delta T_{\rm f}$ , is given by,  $\Delta T_{\rm f} = K_{\rm f} m$ where  $K_{\rm f}$  is the molal freezing point depression and *m* is the molality. The molality is the number of moles of particles dissolved in a kilogram of solvent. If  $\Delta T_{\rm f} = 2.15 \,^{\circ}{\rm C}$  and  $K_{\rm f} = 1.86 \,^{\circ}{\rm C} \,{\rm m}^{-1}$ :  $m = \Delta T_{\rm f} / K_{\rm f} = (2.15 \,{}^{\circ}{\rm C}) / (1.86 \,{}^{\circ}{\rm C} \,{\rm m}^{-1}) = 1.156 \,{\rm m}^{-1} = 1.156 \,{\rm mol} \,{\rm kg}^{-1}$ A mole of NaCl dissolves to give two particles (Na<sup>+</sup> and Cl<sup>-</sup>) so (1.156 / 2) mol = 0.578 mol of NaCl per kilogram of water is needed. As the density of the solution is 1.00 kg  $L^{-1}$ , a kilogram of solution has a volume of one litre. Hence: concentration required =  $0.578 \text{ mol } \text{L}^{-1}$ Answer:  $0.578 \text{ mol } \text{L}^{-1}$ In principle, it would be possible to desalinate this water by pumping it into a cylindrical tower, and allowing gravity to push pure water through a semipermeable membrane at the bottom. At 25 °C, how high would the tower need to be for this to work? (The density of liquid Hg at 25 °C is  $13.53 \text{ g cm}^{-3}$ .) The osmotic pressure,  $\Pi$ , is given by  $\Pi = cRT$  where c is the concentration of the particles. From above,  $c = (2 \times 0.578)$  mol L<sup>-1</sup> and so:  $\Pi = (2 \times 0.578 \text{ mol } \text{L}^{-1}) \times (0.08206 \text{ atm } \text{L mol}^{-1} \text{ K}^{-1}) \times (298 \text{ K}) = 28.3 \text{ atm}$ As 1 atm = 760 mmHg, this corresponds to  $(28.3 \times 760)$  mmHg = 21500 mmHg. Considering the relative densities of water and Hg, the height of water required to exert this pressure would be: 21500 mmHg =  $(21500 \times \frac{13.53}{1.000})$  mmH<sub>2</sub>O = 291000 mmH<sub>2</sub>O or 291 mH<sub>2</sub>O. The tower would need to be 291 m in height. Answer: 291 m

49.0

 $K_{\rm c}(2) = 1/(1.075 \times 10^8)$ 

• At 700 °C, hydrogen and iodine react according to the following equation.

$$H_2(g) + I_2(g) \iff 2HI(g) \qquad K_c =$$

Hydrogen also reacts with sulfur at 700 °C:

 $2H_2S(g) \iff 2H_2(g) + S_2(g)$ 

 $2H_2(g) + S_2(g) \implies 2H_2S(g) \qquad K_c = 1.075 \times 10^8$ 

Determine  $K_c$  for the following overall equilibrium reaction at 700 °C.

 $2I_2(g) + 2H_2S(g) \iff S_2(g) + 4HI(g)$ 

The overall reaction corresponds to the twice the first reaction combined with the reverse of the second reaction:

 $2H_2(g) + 2I_2(g) \iff 4HI(g)$   $K_c(1) = (49.0)^2$ 

 $2I_2(g) + 2H_2S(g) \iff S_2(g) + 4HI(g) \qquad \qquad K_c(3) = K_c(1) \times K_c(2)$ 

The 1<sup>st</sup> reaction is doubled so the original equilibrium constant is squared.

The 2<sup>nd</sup> reaction is reversed so the reciprocal of the equilibrium constant is used.

The two reactions are then combined and the overall equilibrium constant is then the product:

$$K_{\rm c}(3) = K_{\rm c}(1) \times K_{\rm c}(2) = (49.0)^2 \times (1/(1.075 \times 10^8) = 2.23 \times 10^{-5})$$

$$K_{\rm c} = 2.23 \times 10^{-5}$$

What is the standard free energy change at 700 °C for this overall equilibrium reaction?

The equilibrium constant in terms of pressures is first converted into the equilibrium constant in terms of pressures using  $K_p = K_c(RT)^{\Delta n}$ . The reaction involves the conversion of 4 mol of gas to 5 mol of gas so  $\Delta n = +1$  and:

 $K_{\rm p} = K_{\rm c}(RT)^{\Delta n} = (2.23 \times 10^{-5}) \times (0.08206 \times 973)^1 = 0.00178$ 

Note that as  $K_c$  is in terms of concentration units of mol L<sup>-1</sup>, R = 0.08206 atm L mol<sup>-1</sup> K<sup>-1</sup> has been used.

As  $\Delta G^{\circ} = -RT \ln K_{\rm p}$ :

 $\Delta G^{\circ} = -(8.314 \text{ J K}^{-1} \text{ mol}^{-1})^{\circ} (973 \text{ K}) \times \ln(0.00178) = +51.2 \text{ kJ mol}^{-1}$ 

Answer:  $+51.2 \text{ kJ mol}^{-1}$ 

THIS QUESTION CONTINUES ON THE NEXT PAGE.

If 0.250 mol of HI(g) is introduced into a 2.00 L flask at 700 °C, what will be the concentration of  $I_2(g)$  at equilibrium?

The initial concentration of HI(g) is  $0.250 / 2.00 \text{ mol } \text{L}^{-1} = 0.125 \text{ mol } \text{L}^{-1}$ .

	H <sub>2</sub> (g)	I <sub>2</sub> (g)	<del></del>	2HI(g)
Initial	0	0		0.125
Change	+x	+x		-2 <i>x</i>
Equilibrium	x	x		0.125 - 2x

Thus,

$$K_{\rm c} = \frac{[{\rm HI}]^2}{[{\rm H}_2][{\rm I}_2]} = \frac{(0.125 - 2x)^2}{(x)(x)} = \frac{(0.125 - 2x)^2}{x^2} = 49.0 \text{ (from 2008-N-5)}$$

$$(49.0)^{1/2} = \frac{(0.125 - 2x)}{x}$$

Rearranging gives  $x = [I_2(g)] = 0.0139$  M.

Answer: 0.0139 M

If 0.274 g of  $H_2S$  were now introduced into the same flask, what would be the concentration of  $S_2(g)$  at equilibrium?

The molar mass of H<sub>2</sub>S is  $(2 \times 1.008 \text{ (H)} + 32.06 \text{ (S)}) = 34.08 \text{ g mol}^{-1}$ . Hence, 0.274 g of H<sub>2</sub>S corresponds to:

number of moles = mass / molar mass =  $(0.274 \text{ g}) / (34.08 \text{ g mol}^{-1}) = 8.04 \times 10^{-3} \text{ mol}$ 

The initial concentration of H<sub>2</sub>S is thus  $8.04 \times 10^{-3}$  mol / 2.00 M =  $4.02 \times 10^{-3}$  M.

From above,  $[I_2(g)] = 0.0139$  M and  $[HI(g)] = (0.125 - 2 \times 0.0139)$  M = 0.0972 M.

Using the overall equilibrium reaction derived in 2008-N-5:

	2I <sub>2</sub> (g)	2H <sub>2</sub> S(g)	1	<b>S</b> <sub>2</sub> ( <b>g</b> )	4HI(g)
Initial	0.0139	0.00402		0	0.0972
Change	-2x	-2 <i>x</i>		+x	+4x
Equilibrium	0.0139 - 2 <i>x</i>	0.00402 - 2x		x	0.0972 + 4x

### **ANSWER CONTINUES ON THE NEXT PAGE**

Thus,

$$K_{\rm c} = \frac{[S_2][HI]^4}{[I_2]^2[H_2S]^2} = \frac{(x)(0.0972 + 4x)^4}{(0.0139 - 2x)^2(0.00402 - 2x)^2}$$
  

$$\sim \frac{(x)(0.0972)^4}{(0.0139)^2(0.00402)^2} = 2.23 \times 10^{-5} \text{ (from 2008-N-5)}$$
  
where the small x approximation has been used as  $K_{\rm c}$  is so small. This gives:  

$$x = [S_2(g)] = 7.82 \times 10^{-10} \text{ M}$$

Answer:  $7.82 \times 10^{-10}$  M

Marks 6

HF is a weak acid so the equilibrium concentrations need to be calculated using a reaction table:

	HF	+	H <sup>+</sup> (aq)	F <sup>-</sup> (aq)
Initial	0.10		0	0
Change	- <i>x</i>		+x	+x
Equilibrium	0.10 - x		x	x

As  $pK_a = -\log_{10}K_a$ , at equilibrium,

 $K_{\rm a} = \frac{[{\rm H}^+({\rm aq})][{\rm F}^-({\rm aq})]}{[{\rm HF}({\rm aq})]} = \frac{(x)(x)}{(0.10-x)} = \frac{x^2}{(0.10-x)} = 10^{-3.17}$ 

As  $K_a$  is so small, x will be tiny and  $0.10 - x \sim 0.10$  and so

$$x^{2} = 10^{-3.17} \times 0.10$$
 or  $x = [H^{+}(aq)] = 0.00822$  M

As  $pH = -log_{10}[H^+(aq)]$ ,

 $pH = -log_{10}(0.00822) = 2.09$ 

Answer: 2.09

What mass of NaF needs to be added to 100.0 mL of the above solution to make a buffer with a pH of 3.00?

Using the Henderson-Hasselbalch equation for the pH of the buffer:

$$\mathbf{pH} = \mathbf{pK}_{\mathbf{a}} + \log\left(\frac{[\mathbf{base}]}{[\mathbf{acid}]}\right)$$

To make a buffer with pH = 3.00 and [acid] = [HF] = 0.10 M:

$$3.00 = 3.17 + \log\left(\frac{[F^-]}{0.10}\right)$$
 or  $\log\left(\frac{[F^-]}{0.10}\right) = =0.17$ 

Hence,

 $[F^{-}] = 0.10 \times 10^{-0.17} = 0.068 M$ 

The number of moles in 100.0 mL is thus 0.0068 mol. As NaF will dissolve to give one  $F^-$  per formula unit, this is also the number of moles of NaF required.

### ANSWER CONTINUES ON THE NEXT PAGE

The formula mass of NaF is (22.99 (Na) + 19.00 (F)) g mol<sup>-1</sup> = 41.99 g mol<sup>-1</sup>. The mass of NaF required is thus:

mass = number of moles × formula mass =  $(0.0068 \text{ mol}) \times (41.99 \text{ g mol}^{-1}) = 0.28 \text{ g}$ 

Answer: **0.28 g** 

Explain why HCl is a much stronger acid than HF.

Cl is a much larger atom than F and is less electronegative. The H–Cl bond is therefore much longer and weaker than the H–F bond. The H–Cl bond is therefore easier to break and it is the stronger acid.

HF is actually a weak acid. F is smaller and more electronegative than O, so the H–F bond is stronger than the O–H bond. There is consequently little dissociation of HF when it is dissolved in water.

• Cisplatin, [Pt(NH<sub>3</sub>)<sub>2</sub>Cl<sub>2</sub>], is a particularly effective chemotherapy agent against certain types of cancer. Calculate the concentration of Pt<sup>2+</sup>(aq) ions in solution when 0.075 mol of cisplatin is dissolved in 1.00 L of a 1.00 M solution of NH<sub>3</sub>.  $K_{\text{stab}}$  of [Pt(NH<sub>3</sub>)<sub>2</sub>Cl<sub>2</sub>] =  $3.4 \times 10^{12}$ .

The initial concentration of cisplatin when 0.075 mol is dissolved in 1.00 L is 0.075 M.

As  $K_{\text{stab}}$  refers to the formation of the complex, the reaction table is:

	Pt <sup>2+</sup> (aq)	2Cl <sup>-</sup> (aq)	2NH <sub>3</sub> (aq)	-	[Pt(NH <sub>3</sub> ) <sub>2</sub> Cl <sub>2</sub> ]
Initial	0	0	1.00		0.075
Change	+x	+2x	+2x		- <i>x</i>
Equilibrium	x	2x	1.00 + 2x		0.075 - <i>x</i>

Hence:

$$K_{\text{stab}} = \frac{[\text{Pt}(\text{NH}_3)_2\text{Cl}_2]}{[\text{Pt}^{2+}][\text{Cl}^{-}]^2[\text{NH}_3]^2} = \frac{(0.075 - x)}{(x)(2x)^2(1.00 + 2x)^2} = 3.4 \times 10^{12}$$

As  $K_{\text{stab}}$  is so large, x will be very, very small and so  $(1.00 + 2x) \sim 1.00$  and  $(0.075 - x) \sim 0.075$ . With this:

$$K_{\text{stab}} \sim \frac{(0.075)}{(x)(2x)^2(1.00)^2} = \frac{(0.075)}{(4x)^3} = 3.4 \times 10^{12}$$
  
 $x = [\text{Pt}^{2+}(\text{aq})] = 1.8 \times 10^{-5} \text{ M}$ 

Answer: **1.8** × **10<sup>-5</sup>** M

What changes would occur to the values of  $K_{\text{stab}}$  for cisplatin and the concentration of  $Pt^{2+}(aq)$  ions if solid KCl were dissolved in the above solution?

K <sub>stab</sub>	increase	no change	decrease
[Pt <sup>2+</sup> (aq)]	increase	no change	<u>decrease</u>

(i)  $K_{\text{stab}}$  is the stability constant – it is a constant at any given temperature.

(ii) From Le Chatelier's principle, if [Cl<sup>-</sup>(aq)] is increased then the equilibrium will shift to the right and so [Pt<sup>2+</sup>(aq)] will decrease.

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Marks • A galvanic cell is made of a  $Zn^{2+}/Zn$  half cell with  $[Zn^{2+}] = 2.0$  M and an Ag<sup>+</sup>/Ag half cell with  $[Ag^{+}] = 0.050$  M. Calculate the electromotive force of the cell at 25 °C.

The standard reduction reactions and potentials for the two half cells are:

$$Zn^{2+}(aq) + 2e^{-} \rightarrow Zn(s) \qquad E^{\circ} = -0.76 V$$
  
Ag<sup>+</sup>(aq) + e<sup>-</sup>  $\rightarrow$  Ag(s) 
$$E^{\circ} = +0.80 V$$

The least positive  $(Zn^{2+}/Zn)$  couple is reversed giving the overall reaction:

$$Zn(s) + 2Ag^{+}(aq) \rightarrow Zn^{2+}(aq) + 2Ag(s)$$
  $E^{\circ} = (+0.76 \text{ V}) + (0.80) = 1.56 \text{ V}$ 

As non-standard concentrations are used, the cell potential is calculated using the Nernst equation. The reaction involves the transfer of  $2e^{-1}$  so with n = 2 this becomes:

$$E = E^{\circ} - \frac{RT}{nF} \ln Q = E^{\circ} - \frac{RT}{nF} \ln \left( \frac{[\text{Zn}^{2+}(\text{aq})]}{[\text{Ag}^{+}(\text{aq})]^{2}} \right)$$
  
= (+1.56 V) -  $-\frac{(8.314 \text{ J K}^{-1} \text{ mol}^{-1})(298 \text{ K})}{(2 \times 96485 \text{ C mol}^{-1})} \ln \left( \frac{2.0}{0.050^{2}} \right) = +1.47 \text{ V}$   
Answer: +1.47 V

Calculate the equilibrium constant of the reaction at 25 °C.

The equilibrium constant is related to the standard cell potential:

$$E^{\circ} = \frac{RT}{nF} \ln K$$

Hence,

$$\ln K = E^{\circ} \times \frac{nF}{RT} = (1.56 \text{ V}) \times \frac{(2 \times 96485 \text{ C mol}^{-1})}{(8.314 \text{ J K}^{-1} \text{ mol}^{-1})(298 \text{ K})} = 121.5$$
$$K = 5.9 \times 10^{52}$$

Answer:  $K = 5.9 \times 10^{52}$ 

Calculate the standard Gibbs free energy of the reaction at 25 °C.

Using 
$$\Delta G^{\circ} = nFE^{\circ}$$
:  
 $\Delta G^{\circ} = -(2 \times 96485 \text{ C mol}^{-1}) \times (+1.56 \text{ V}) = -301 \text{ kJ mol}^{-1}$   
Answer: -301 kJ mol<sup>-1</sup>

Indicate whether the reaction is spontaneous or not. Give a reason for your answer.

### As E > 0, $\Delta G^{\circ} < 0$ and K is very large: the reaction is spontaneous.

Express the overall reaction in the shorthand voltaic cell notation.

# $Zn(s) | Zn^{2+}(aq) (2.0 M) | | Ag^{+}(aq) (0.050 M) | Ag(s)$

Marks • Strontium-90 is one of the harmful nuclides resulting from nuclear fission explosions. 3 Strontium-90 decays by beta particle emission with a half-life of 28.0 years. How long (in years) would it take for 99.0% of a sample of strontium-90 released in an atmospheric test of an atomic bomb to decay? The number of nuclei at time t,  $N_t$ , is related to the number of nuclei present at  $t = 0, N_0$  by:  $\ln\left(\frac{N_0}{N_t}\right) = \lambda t$ where  $\lambda$  is the activity constant. The half life,  $t_{1/2}$ , corresponds to the time required for half of the sample to decay:  $\frac{N_0}{N_t} = 2$  and so  $t_{1/2} = \frac{\ln 2}{\lambda}$ . Hence,  $\lambda = \frac{\ln 2}{t_{1/2}}$ If 99.0% of the sample has decayed, 1.0% is remaining and so  $\frac{N_0}{N_*} = \frac{100}{1}$ :  $\ln\left(\frac{100}{1}\right) = \frac{\ln 2}{(28.0 \text{ vears}^{-1})} \times t \text{ or } t = 186 \text{ years.}$ Answer: 186 years • A standard test for the presence of chloride ion in water involves the appearance of a 3 precipitate of AgCl upon addition of 0.05 mL of AgNO<sub>3</sub> (0.03 M) to 100 mL of sample. What is the minimum concentration of Cl<sup>-</sup> detectable by this method?

The  $K_{\rm sp}$  of AgCl =  $1.8 \times 10^{-10}$ .

The number of moles of  $Ag^+(aq)$  in 0.05 mL of a 0.03 M solution of  $AgNO_3(aq)$  is:

number of moles = concentration × volume =  $(0.03 \text{ mol } \text{L}^{-1}) \times (0.05 \times 10^{-3} \text{ L}) = 1.5 \times 10^{-6} \text{ mol}$ 

When this is added to 100. mL of the sample:

 $[Ag^{+}(aq)] =$  number of moles / volume = (1.5 × 10<sup>-6</sup> mol) / (0.100 L) = 1.5 × 10<sup>-5</sup> M

For AgCl(s),  $K_{sp} = [Ag^+(aq)][Cl^-(aq)]$  and so:

 $[C\Gamma(aq)] = K_{sp} / [Ag^+(aq)] = 1.8 \times 10^{-10} / 1.5 \times 10^{-5} = 1.2 \times 10^{-5}$ 

Answer:  $1.2 \times 10^{-5}$ 

Marks

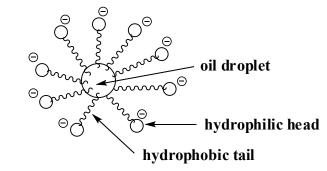
2

• Explain how soap acts to remove oil.

Soap molecules consist of a long hydrophobic tail and a charged hydrophilic head.

The molecules are able to form micelles (see diagram below) in which the tails interact with the oil particles and the heads interact with the water.

In this way, the oil is dissolved in the water and can be removed.



• A melt of NaCl is electrolysed for 35 minutes with a current of 3.50 A. Calculate the mass of sodium and volume of chlorine at 40 °C and 1.00 atm that are formed.

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The number of moles of electrons delivered by a current, *I*, of 3.50 A in 35 minutes is:

number of moles of electrons = 
$$\frac{It}{F} = \frac{(3.50 \text{ A})(35 \times 60 \text{ s})}{(96485 \text{ C mol}^{-1})} = 0.076 \text{ mol}$$

The overall electrolysis reaction, NaCl(l)  $\rightarrow$  Na(s) +  $\frac{1}{2}Cl_2(g)$ , corresponds to reduction of Na<sup>+</sup> and oxidation of Cl<sup>-</sup>:

 $Na^+ + e^- \rightarrow Na$  and  $Cl^- \rightarrow \frac{1}{2}Cl_2 + e^-$ 

As one mole of electrons would produce one mole of Na and half a mole of Cl<sub>2</sub>:

number of moles of Na = 0.076 mol

number of moles of  $Cl_2 = \frac{1}{2} \times 0.076$  mol = 0.038 mol

The mass of Na produced is therefore:

mass of Na = number of moles × atomic mass

 $= (0.076 \text{ mol}) \times (22.99 \text{ g mol}^{-1}) = 1.8 \text{ g}$ 

Using the ideal gas law, PV = nRT, the volume of Cl<sub>2</sub> produced is:

$$V = \frac{nRT}{P} = \frac{(0.038 \text{ mol})(0.08206 \text{ L atm } \text{K}^{-1} \text{ mol}^{-1})(313 \text{ K})}{(1.00 \text{ atm})} = 0.98 \text{ L}$$

potential energy

Marks • Draw the potential energy diagram for an endothermic reaction. Indicate on the 3 diagram the activation energy for both the forward and reverse reaction, and the enthalpy of reaction.  $E_a$  backward rection products reactants  $\Delta H$  $E_{\rm a}$  forward reaction reaction coordinate As the reaction is endothermic, the energy of the products is higher than that of the reactants. 4 Consider the reaction:  $NO_2(g) + CO(g) \rightarrow NO(g) + CO_2(g)$ The experimentally determined rate equation is: Rate =  $k[NO_2(g)]^2$ Show the rate expression is consistent with the following mechanism: Step 1  $2NO_2(g) \iff N_2O_4(g)$ fast Step 2  $N_2O_4(g) \rightarrow NO(g) + NO_3(g)$ slow Step 3  $NO_3(g) + CO(g) \rightarrow NO_2(g) + CO_2(g)$ fast

Step 2 is rate determining step and this will determine the rate of the reaction. The subsequent step can be ignored in working out the rate.

Step 2 involves the decomposition of  $N_2O_4$  and depends only on its concentration:

rate =  $k_2[N_2O_4(g)]$ 

As this involves the concentration of a reaction intermediate, it is not experimentally testable. The rate law should only involve the concentration of reactants, as their concentrations can be controlled.

As step 2 is slow, step 1 will be able to reach rapid equilibrium.

The forward reaction involves two NO<sub>2</sub> molecules reacting so has a rate:

rate of forward reaction =  $k_1 [NO_2(g)]^2$ 

## ANSWER CONTINUES ON THE NEXT PAGE

The backward reaction involves the decomposition of  $N_2O_4$  and so depends only on its concentration:

rate of backward reaction =  $k_{-1}[N_2O_4(g)]$ 

If step 1 is at equilibrium then the rate of the forward and backward reactions will be equal:

$$k_1[NO_2(g)]^2 = k_{-1}[N_2O_4(g)]$$
 or  $[N_2O_4(g)] = \frac{k_1}{k_{-1}}[NO_2(g)]^2 = K_{eq}[NO_2(g)]^2$ 

Using this expression for [N<sub>2</sub>O<sub>4</sub>(g)] gives:

rate = 
$$k_2[N_2O_4(g)] = \frac{k_1k_2}{k_{-1}} [NO_2(g)]^2$$
 or rate =  $k_2K_{eq}[NO_2(g)]^2$ 

This is consistent with the experiment rate law with  $k = \frac{k_1 k_2}{k_{-1}} = k_2 K_{eq}$ .

- Marks
  - 2
- A concentration cell containing aqueous solutions of Cu(NO<sub>3</sub>)<sub>2</sub> and solid copper metal is constructed so that the Cu<sup>2+</sup> ion concentration in the cathode half-cell is 0.66 M. Calculate the concentration of the Cu<sup>2+</sup> ion in the anode half-cell if the cell potential for the concentration cell at 25 °C is 0.03 V.

The cathode and anode reactions are:  $Cu^{2+}(aq) + 2e^{-} \Rightarrow Cu(s) \quad (cathode)$   $Cu(s) \Rightarrow Cu^{2+}(aq) + 2e^{-} \quad (anode)$ The standard electrode potential  $E^{\circ} = 0$  V and the potential can be calculated using the Nernst equation for this 2 electron reaction, n = 2:  $E = E^{\circ} - \frac{RT}{nF} \ln Q = -\frac{RT}{nF} \ln \left( \frac{[Cu^{2+}(aq)]_{anode}}{[Cu^{2+}(aq)]_{anode}} \right)$   $= -\frac{(8.314 \text{ J K}^{-1} \text{ mol}^{-1})(298 \text{ K})}{(2 \times 96485 \text{ C mol}^{-1})} \ln \left( \frac{[Cu^{2+}(aq)]_{anode}}{0.66} \right) = +0.03 \text{ V}$ This gives  $[Cu^{2+}(aq)]_{anode} = 0.06 \text{ M}.$ 

• In **acid solution**, dichromate ion oxidises iron(II) to iron(III) as illustrated in the partial equation:

 $Fe^{2+} + Cr_2O_7^{2-} \rightarrow Fe^{3+} + Cr^{3+}$ 

Answer: 0.06 M

Write a balanced equation for this reaction.

The half reactions are:

$$Fe^{2^+} \rightarrow Fe^{3^+} + e^-$$
  
 $Cr_2O_7^{2^-} + 14H^+ + 6e^- \rightarrow 2Cr^{3^+} + 7H_2O$ 

where  $H^+$  has been added to the  $Cr_2O_7^{2-} / Cr^{3+}$  couple to give  $H_2O$ .

To balance the electrons, the first reaction needs to be multiplied by 6. Hence:

$$6Fe^{2+} + Cr_2O_7^{2-} + 14H^+ \rightarrow 6Fe^{3+} + 2Cr^{3+} + 7H_2O$$

What would happen to the cell potential if the concentration of  $Cr^{3+}$  were increased?

It would decrease. If [Cr<sup>3+</sup>] is increased, Le Châtelier's principle predicts that the reaction will shift towards reactants, reducing the cell potential.

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• Nitric oxide reacts with ozone according to the following equation.

$$NO(g) + O_3(g) \rightarrow NO_2(g) + O_2(g)$$

The following rate data were collected at a specified temperature.

Trial	Initial[NO] (M)	Initial [O <sub>3</sub> ] (M)	Initial rate of reaction (M $s^{-1}$ )
1	$2.1  imes 10^{-6}$	$2.1  imes 10^{-6}$	$1.6  imes 10^{-5}$
2	$6.3  imes 10^{-6}$	$2.1  imes 10^{-6}$	$4.8  imes 10^{-5}$
3	$6.3  imes 10^{-6}$	$4.2  imes 10^{-6}$	$9.6 \times 10^{-5}$

What is the experimental rate law for the reaction?

Rate =  $k[NO]^{x}[O_{3}]^{y}$ 

Between trials (1) and (2),  $[O_3]_{initial}$  is constant and  $[NO]_{initial}$  is tripled. This leads to the rate tripling: x = 1.

Between trials (2) and (3),  $[NO]_{initial}$  is constant and  $[O_3]_{initial}$  is doubled. This leads to the rate doubling: y = 1.

Hence:

rate =  $k[NO][O_3]$ 

What is the value of the rate constant of this reaction?

Using trial (1),

$$k = \frac{\text{rate}}{[\text{NO}][\text{Cl}]} = \frac{1.6 \times 10^{-5} \text{ M s}^{-1}}{(2.1 \times 10^{-6} \text{ M})(2.1 \times 10^{-6} \text{ M})} = 3.6 \times 10^{6} \text{ M}^{-1} \text{ s}^{-1}$$

Answer:  $3.6 \times 10^{6} \text{ M}^{-1} \text{ s}^{-1}$ 

• Explain why surface effects are important in colloidal systems.

The small size of the colloidal particles means that they have a very large total surface area.

The colloid can be stabilised by steric and/or electrostatic effects.

If surface interactions are unfavourable, they are minimised by flocculation and coagulation.

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