Topics in the June 2006 Exam Paper for CHEM1901

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- Bonding in H₂ MO theory
- Bonding in O2, N2, C2H2, C2H4 and CH2O
- Band Theory MO in Solids

2006-J-3:

- Nuclear and Radiation Chemistry
- Wave Theory of Electrons and Resulting Atomic Energy Levels

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• Ionic Bonding

2006-J-5:

Bonding in O₂, N₂, C₂H₂, C₂H₄ and CH₂O

2006-J-6:

- Lewis Structures
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- Wave Theory of Electrons and Resulting Atomic Energy Levels

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• Equilibrium and Thermochemistry in Industrial Processes

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• First and Second Law of Thermodynamics

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• In the spaces provided, explain the meaning of the following terms. You may use an example, equation or diagram where appropriate.

Marks 6

(a) Pauli exclusion principle

The principle that states that no two electrons in an atom or molecule can have the same set of quantum numbers. It limits the number of electrons that can occupy an orbital to two.

(b) electronegativity

The ability of an atom to attract electron density towards itself in a covalent bond. Fluorine is the most electronegative element.

(c) ionic bond

The low energy state found in ionic solids associated with the Coulombic attraction of unlike charged ions.

(d) paramagnetic

A property of an atom, ion, molecule or solid resulting from the presence of at least one unpaired electron spin Paramagnets are attracted towards a magnetic field.

(e) n-type semiconductor

A semiconductor has electrical conductivity in between that of a metal and that of an insulator. A n-type semiconductor is obtained by adding a type of atoms to a semiconductor in order to increase the number of negative charge carrier. For example, doping a group 14 element such as Si with a group 15 element such as As leads to extra electrons in the conductance band which are free to move and carry the charge.

(e) σ bond

A bond produced by the occupation of a σ -bonding molecular orbital. This orbital is made by overlap of atomic orbitals, such as end-on/end-on overlap of p-orbitals or of s-orbitals, to produce a molecular orbital with no nodes along the internuclear axis. The electron density is along the internuclear axis.

• Balance the following nuclear reactions by identifying the missing nuclide.

$$^{55}_{26} \text{Fe} + {^{0}_{-1}} \text{e} \rightarrow$$
 $^{55}_{25} \text{Mn}$

$$^{63}_{28}$$
Ni \rightarrow $^{63}_{29}$ Cu + $^{0}_{-1}\beta$

$$^{28}_{14}\mathrm{Si} + ^{2}_{1}\mathrm{H} \rightarrow ^{1}_{0}\mathrm{n} +$$
 $^{29}_{15}\mathrm{P}$

• Identify the decay mechanism for the following three unstable nuclides given that the only stable isotopes of Pr and Eu are $^{141}_{59}$ Pr , $^{151}_{63}$ Eu and $^{153}_{63}$ Eu. There are no stable isotopes of Rn.

Isotope	Nuclear Decay Mechanism
¹⁴² ₅₉ Pr	Stable nucleus has fewer neutrons: <u>β decay</u>
¹⁵⁰ ₆₃ Eu	Stable nucleus has more neutrons: β ⁺ decay or e ⁻ capture
²²² ₈₆ Rn	α decay

• Identify two specific features of atomic structure that can only be explained by reference to the wave-like nature of electrons. Give reasons.

Electrons occupy certain stable "orbits" that correspond to the standing waves obtained by solving the Schrödinger Equation. Each solution (orbital) corresponds to a different allowed energy level. As a consequence of this;

- electrons do not spiral in towards the nucleus despite the electrostatic attraction between them
- the light emitted by excited atoms is a series of discrete spectral lines corresponding to the energy differences between the allowed energy states.

Marks

3

3

2

1

• The ionic solids NaCl, LiF, KF and LiCl, all have the same crystal structure. Assuming only electrostatic interactions are involved, use the information below to organise these four ionic solids in order of increasing energy of the crystal lattice.

ion	radius (10 ⁻¹² m)	ion	radius (10 ⁻¹² m)
Li ⁺	76	F^-	133
Na ⁺	102	Cl ⁻	181
K ⁺	138		

Working

The electrostatic attraction between the cations and anions in an ionic solid depends on:

- The ionic charges: higher cation and anion charges lead to higher lattice energies. In these systems, the cations are all +1 and the anions all -1.
- The lattice structure: higher coordination numbers lead to higher Madelung constants and higher lattice energies. These systems all adopt the same structure (the rocksalt or NaCl structure).
- The separation of the cations and anions: higher ionic radii lead to longer separations and lower lattice energies.

The cation – anion separation is given by the sum of the ionic radii:

• NaCl: (102 + 181) = 283 pm, LiF: (76 + 133) = 209 pm, KF: (138 + 133) = 271 pm, LiCl: (76 + 181) = 257 pm.

The order of the lattice energies is the same as that of these separations.

Increasing energy of the crystal lattice \rightarrow

NaCl	KF	LiCl	LiF
NaCi	Kr	Lici	Lir

• Explain why CsCl, NaCl and ZnS have different crystal structures.

The lattice energy is higher when the number of cations around the anions and the number of anions around the cations are both maximised. The relative sizes of the ions controls how many can be fitted around each one.

 \mathbf{Cs}^+ is the largest cation and can fit 8 \mathbf{Cl}^- ions around it.

Na⁺ is smaller and can only fit 6 Cl⁻ ions around it.

 Zn^{2+} is even smaller and S^{2-} is larger than Cl^- so that only 6 anions can fit around the cation.

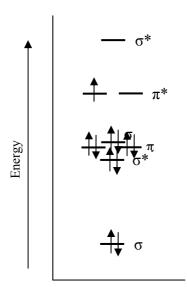
These 'radius – ratio' rules work best in very ionic systems. In those where covalency is also important, orbital overlap can also play a role. For example, ZnS is likely to be significantly more covalent than the alkali metal chlorides. The tetrahedral coordination of \mathbf{Zn}^{2+} in ZnS may be partly due to covalency.

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• The molecular orbital energy level diagram below is for the valence electrons of the ${\rm O_2}^+$ ion.

Marks 4

Indicate the ground state electronic configuration of ${\rm O_2}^+$ using the arrow notation for electron spins on the provided molecular orbital energy level diagram.



Calculate the bond order of O_2^+ .

Bond order =
$$\frac{1}{2}(8-3) = 2.5$$

Indicate the lowest energy electron excitation in this ion by identifying the initial and final molecular states of the electron undergoing the excitation.

The gap between the highest occupied σ and the π^* is very similar to that between π^* and σ^* : either $\sigma \to \pi^*$ or $\pi^* \to \sigma^*$

• Consider the molecule whose structure is shown below. Complete the table concerning the atoms **A**, **B** and **C** indicated by the arrows.

Marks 3

Selected atom	Number of lone pairs about the selected atom	Number of σ-bonds associated with the selected atom	Geometry of σ-bonds about the selected atom
A	1	2	bent
В	0	3	trigonal planar
C	1	3	trigonal pyramidal

• Calculate the energy (in J) and the wavelength (in nm) of the photon of radiation emitted when the electron in Be³⁺ drops from an n = 3 state to an n = 2 state.

Be³⁺ has only 1 e⁻ so the equation $E_n = \frac{-E_R Z^2}{n^2}$ where $E_R = 2.18 \times 10^{-18} J$ can be used. Be has Z = 4.

The energy of the n = 3 and n = 2 levels are:

$$E_3 = \frac{-E_R(4)^2}{(3)^2} = -\frac{16}{9}E_R$$
 and $E_2 = \frac{-E_R(4)^2}{(2)^2} = -\frac{16}{4}E_R = -4E_R$

The energy separation is $\frac{20}{9}$ E_R = $\frac{20}{9}$ × (2.18 × 10⁻¹⁸) = 4.84 × 10⁻¹⁸ J

As
$$E = \frac{hc}{\lambda}$$
,

$$\lambda = \frac{hc}{E} = \frac{(6.634 \times 10^{-34}) \times (2.998 \times 10^8)}{(4.84 \times 10^{-18})} = 4.11 \times 10^{-8} \text{ m} = 41.1 \text{ nm}$$

Energy =
$$4.84 \times 10^{-18} \text{ J}$$

Wavelength = **41.1** nm

3

• Write the equation whose enthalpy change represents the standard enthalpy of formation of hydrazine, N₂H₄(g).

Marks 4

$$N_2(g) + 2H_2(g) \rightarrow N_2H_4(g)$$

Write the equation whose enthalpy change represents the enthalpy of combustion of hydrazine, $N_2H_4(g)$ to produce water vapour.

$$N_2H_4(g) + O_2(g) \rightarrow N_2(g) + 2H_2O(g)$$

Given the following data, calculate the standard enthalpy of formation of $N_2H_4(g)$.

$$\Delta H^{\circ}_{f} (H_{2}O(g)) = -242 \text{ kJ mol}^{-1}$$

 $\Delta H^{\circ}_{comb} (N_{2}H_{4}(g)) = -580 \text{ kJ mol}^{-1}$

Using $\Delta_{rxn}H^0=\sum m\Delta_fH^0$ (products) $-\sum n\Delta_fH^0$ (reactants), the enthalpy change for the combustion reaction is:

 $\Delta_{comb}H^0=[2\Delta_fH^0(H_2O(g))]-[\Delta_fH^0(N_2H_4(l))] \ as \ the \ remaining \\ compounds \ are \ elements \ in \ their \ standard \ states.$

Hence:

$$[2 \times -242] - [\Delta_f H^o(N_2 H_4(l))] = -580 \text{ kJ mol}^{-1}$$

 $\Delta_f H^o(N_2 H_4(l))] = +96 \text{ kJ mol}^{-1}$

Answer: +96 kJ mol⁻¹

• Estimate the temperature of Mars given its radius of 3400 km and the solar power density at its surface of 590 J m⁻² s⁻¹. Assume an average albedo of 16% and zero Greenhouse effect.

With an average albedo of 16%, 94% of the solar energy is not reflected. As the solar power density is 590 J m⁻² s⁻¹:

$$E_{in} = \pi r^2 \times 590 \times 0.84$$

$$E_{out} = 4\pi r^2 \times (5.67 \times 10^{-8}) \times T^4$$

As $E_{out} = E_{in}$:

$$T^4 = \frac{590 \times 0.84}{4 \times 5.67 \times 10^8}$$
 or $T = 216$ K.

3

• In an experiment, 1.76 g of sodium nitrate was dissolved in water inside a calorimeter. Give a balanced equation for the reaction that took place.

Marks 4

$$NaNO_3(s) \rightarrow Na^+(aq) + NO_3^-(aq)$$

The temperature of the solution was found to decrease by 1.22 °C. If the heat capacity of the calorimeter was 77.0 J K^{-1} and the heat capacity of the solution was 268 J K^{-1} , determine the molar heat of reaction.

The heat change is given by:

$$q = (c_{calorimeter} \times \Delta T) + (c_{solution} \times \Delta T) = (77.0 \times 1.22) + (268 \times 1.22) = 421 \text{ J}$$

The process is endothermic as the temperature of the solution decreases.

The molar mass of NaNO₃ is
$$(22.99 (Na)) + (14.01 (N)) + (3 \times 16.00 (O)) = 85$$

The molar heat of reaction is therefore:

$$q_m = \frac{85}{1.76} \times 421 = 20300 \text{ J mol}^{-1} = 20.3 \text{ kJ mol}^{-1}$$

Answer: 20.3 kJ mol⁻¹

How long would it take a 250 W power supply to reheat the calorimeter to its starting temperature?

A 250 W power supply delivers 250 J s $^{-1}$. As 410 J was removed from the calorimeter and the water inside it to reduce the temperature by 1.22 $^{\circ}$ C, the power suppy will take:

$$t = \frac{421}{250} = 1.68 \,\mathrm{s}$$

• At 773 K, the following reaction has an equilibrium constant, K_p , of 1.52×10^{-5} atm⁻².

Marks

$$N_2(g) + 3H_2(g) \rightleftharpoons 2NH_3(g)$$

If 0.0200 mol of ammonia were introduced into an evacuated 1.00 L container at 773 K, what would be the partial pressures of N_2 , H_2 and NH_3 at equilibrium?

The initial pressure of ammonia can be calculated using the ideal gas law:

$$\mathbf{p}_{\text{NH}_3} = \frac{\mathbf{nRT}}{\mathbf{V}} = \frac{(0.0200) \times (0.08206) \times 773}{1.00} = 1.27$$

The reaction table is:

	$N_2(g)$	$3H_2(g)$		$2NH_3(g)$
start	0	0		1.27
change	X	3x		-2x
equilibrium	X	3x		1.27 - 2x

$$\mathbf{K}_{p} = \frac{(\mathbf{p}_{NH_{3}})^{2}}{(\mathbf{p}_{NH_{3}})^{3}(\mathbf{p}_{H_{3}})} = \frac{(1.27 - 2x)^{2}}{(x)(3x)^{3}} = \frac{(1.27 - 2x)^{2}}{27x^{4}} = 1.52 \times 10^{-5}$$

As K_p is small, x will be \emph{large} and hence no approximation can be made. The equation rearranges to:

$$(1.27-2x)^2 = (1.52 \times 10^{-5}) \times 27x^4$$

so

$$(1.27-2x) = (2.03 \times 10^{-2})x^2$$
 or $(2.03 \times 10^{-2})x^2 + 2x - 1.27 = 0$

This must be solved with the quadratic equation using $a = (2.03 \times 10^{-2})$, b = 2 and c = -1.27:

$$x = \frac{-b + \sqrt{b^2 - 4ac}}{2a} = \frac{-2 + \sqrt{(2)^2 - (4 \times 2.03 \times 10^{-3} \times -1.27)}}{(2 \times (2.03 \times 10^{-2}))} = 0.631$$

Only the positive root has a physical relevance for the equilibrium. Hence:

$$p_{\rm N_2} = x = 0.631 \ atm, \ p_{\rm H_2} = 3x = 1.89 \ atm \ and \ \ p_{\rm NH_3} = (1.27\text{-}2x) = 8.07 \times 10^{\text{-}3} \ atm$$

$P(N_2) = 0.631$ atm	$P(H_2) = 1.89 \text{ atm}$	$P(NH_3) = 8.07 \times 10^{-3}$ atm
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Marks 3

• Refer to the electrochemical potentials on the data sheet.

Show that $Fe^{2+}(aq)$ is not stable under 1 atm O_2 in a 1 M solution of HCl. What happens to Fe^{2+} ?

 Fe^{2+} will be oxidised by O_2 under these conditions. The relevant half cells are:

The overall reaction is:

$$4Fe^{2+}(aq) + O_2(g) + 4H^+(aq) \rightarrow 4Fe^{3+}(aq) + 2H_2O$$

$$E^{\circ} = -0.77 + 1.23 = +0.46$$

As $E^{\circ} > 0$, the reaction is spontaneous.

Show Fe(s) is stabilised by galvanizing with Zn(s).

The electrode potentials for oxidation of Fe(s) and Zn(s) are:

As Zn(s) has a higher oxidation potential, it will be preferentially oxidised and will therefore protect Fe(s).

Show Cu⁺(aq) is not stable in water. What would happen to Cu⁺(aq)?

The electrode potential for reduction of Cu⁺(aq) is:

$$Cu^{+}(aq) + e^{-} \rightarrow Cu(s)...$$
 $E^{\circ} = +0.53 \text{ V}$

The electrode potential for oxidation of Cu(s) is:

$$Cu(s) \rightarrow Cu^{2+}(aq) + 2e^{-}...E^{\circ} = -0.34 \text{ V}$$

The reaction:

$$2Cu^{+}(aq) \rightarrow Cu(s) + Cu^{2+}(aq)$$

therefore has an overall potential of $E^{\circ} = (+0.53) + (-0.34) = +0.17 \text{ V}$

This disproportionation reaction has $E^{\circ} > 0$ and is spontaneous.

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• In the chlor-alkali process H₂(g), OH⁻(aq) and Cl₂(g) are produced by the electrolysis of a concentrated solution of sodium chloride. Explain how hydrogen gas is produced at the cathode, and why chlorine gas rather than oxygen gas forms at the anode.

Marks 6

At the cathode, water is reduced to H_2 rather than sodium being reduced to Na metal due to the relative size of the reduction potentials:

Na⁺(aq) + e⁻ → Na(s)
$$E^{\circ}_{red} = -2.71 \text{ V}$$

2H₂O(l) + 2e⁻ → H₂(g) + 2OH⁻(aq) $E^{\circ}_{red} = -0.83 \text{ V}$

Reduction of water has a more favourable (less negative) reduction potentials and is reduced preferentially.

At the anode, the relevant oxidation potentials are:

$$2Cl^{-}(aq) \rightarrow Cl_{2}(g) + 2e^{-}$$
 $E^{\circ}_{ox} = -1.36 \text{ V}$
 $2H_{2}O(l) \rightarrow O_{2}(g) + 4H^{+}(aq) + 4e^{-}$ $E^{\circ}_{ox} = -1.23 \text{ V}$

Oxidation of $H_2O(1)$ has a more favourable oxidation potential so it appears that it should be preferentially oxidised. However, the overpotential for the formation of $O_2(g)$ is *much* greater than the overpotential for the formation of $Cl_2(g)$. As a result, it is actually $Cl_2(g)$ that is produced rather than $O_2(g)$.

A chlor-alkali plant produces 42.3 tonne of Cl_2 per day. Calculate the minimum current used. (1 tonne = 1000 kg)

42.3 tonne corresponds to 42.3×10^3 kg or 42.3×10^6 g. The molar mass of Cl_2 is $(2 \times 35.45) = 70.9$. The number of moles of Cl_2 produced each day is therefore:

number of moles =
$$\frac{\text{mass}}{\text{molar mass}} = \frac{42.3 \times 10^6}{70.9} = 5.97 \times 10^5 \text{ mol.}$$

The half cell reaction for production of $Cl_2(g)$ is $2Cl^-(aq) \rightarrow Cl_2(g) + 2e^-$

Production of 1 mol of $Cl_2(g)$ requires 2 mol of electrons so the daily production requires $2 \times (5.97 \times 10^5) = 1.19 \times 10^6$ mol.

The number of moles of electrons delivered by a current I is given by:

$$\mathbf{n} = \frac{\mathbf{Q}}{\mathbf{F}} = \frac{\mathbf{I}\mathbf{t}}{\mathbf{F}}$$

A day corresponds to $t = (24 \times 60 \times 60) = 86400$ seconds. The current required to generate 1.19×10^6 mol of electrons is therefore:

$$I = \frac{n \times F}{t} = \frac{(1.19 \times 10^6) \times (96485)}{(86400)} = 1.33 \times 10^6 \text{ A}$$

Answer: 1.33×10^6 A

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Calculate the amount of H_2 produced (in mol) and estimate the daily energy available to the plant through combustion of this hydrogen. $\Delta H^{\circ}_{f}(H_2O(g)) = -242 \text{ kJ mol}^{-1}$

 $H_2(g)$ is produced through the reaction $2H_2O(l) + 2e^- \rightarrow H_2(g) + 2OH^-(aq)$.

The number of moles of $H_2(g)$ is the same as that for $\operatorname{Cl}_2(g) = 5.97 \times 10^5$ mol.

Combustion of H₂ follows the reaction:

$$H_2(g) + \frac{1}{2}O_2(g) \rightarrow H_2O(g)$$

Hence, $\Delta_{\text{comb}}H^{\circ}(\text{H}_2(g)) = \Delta_f H^{\circ}(\text{H}_2\text{O}(g)) = -242 \text{ kJ mol}^{-1}$.

Assuming 100% efficiency, combustion of 5.97×10^5 mol therefore generates:

$$\Delta_{comb}H = (5.97 \times 10^5) \times (-242) = 1.44 \times 10^8 \text{ kJ.}$$

Answer: $1.44 \times 10^8 \text{ kJ}$

• State the Second Law of Thermodynamics, and explain how the enthalpy of reaction is related to the entropy change of the surroundings.

2006-J-12

Marks 5

The entropy of the universe always increases: $\Delta_{univ}S = \Delta_{svs}S + \Delta_{surr}S > 0$

The surroundings act as a reservoir of heat for the system: heat gained or lost in a reaction is taken or given to the surroundings, respectively.

As $\Delta_{sys}H = -q_{surr}$ at constant pressure:

$$\Delta_{surr}S = \frac{\mathbf{q}_{surr}}{\mathbf{T}} = \frac{-\Delta_{sys}H}{\mathbf{T}}$$

Give an example of a chemical reaction or a chemical process that corresponds to each of the following.

$$\Delta S > 0$$
, $\Delta H > 0$

As $\Delta_{surr}S = \frac{-\Delta_{sys}H}{T} < 0$, such processes will only occur if the temperature is sufficiently *high* that $\Delta_{surr}S$ is smaller in magnitude than $\Delta_{sys}S$.

Examples include:

- Melting of ice at 300 K: $H_2O(s) \rightarrow H_2O(l)$
- Boiling of water at 400 K: $H_2O(1) \rightarrow H_2O(g)$
- $NH_4NO_3(s) \rightarrow NH_4^+(aq) + NO_3^-(aq)$

 $\Delta S > 0$, $\Delta H < 0$

As
$$\Delta_{surr}S = \frac{-\Delta_{sys}H}{T} > 0$$
 and $\Delta_{sys}S > 0$, such processes will occur at all

temperatures. Examples include:

- Burning of ethane: $2C_2H_6(g) + 7O_2(g) \rightarrow 4CO_2(g) + 6H_2O(g)$
- $CaCl_2(s) \rightarrow Ca^{2+}(aq) + 2Cl^{-}(aq)$

 $\Delta S < 0, \Delta H < 0$

As
$$\Delta_{surr}S = \frac{-\Delta_{sys}H}{T} > 0$$
, such processes will only occur if the temperature is

sufficiently low that $\Delta_{surr}S$ is larger in magnitude than $\Delta_{sys}S$.

Examples include:

- Freezing of ice at 263 K: $H_2O(l) \rightarrow H_2O(s)$
- Condensing of steam at 300 K: $H_2O(g) \rightarrow H_2O(l)$